

IDS 702: MODULE 2.3

LOGISTIC REGRESSION WITH ONE PREDICTOR (ILLUSTRATION)

DR. OLANREWAJU MICHAEL AKANDE

PREDICTING NBA WINS

- Let's fit a logistic regression with one predictor to NBA data for four seasons from the 2014/2015 season to the 2017/2018 season.
- Suppose we want to see how the amount of points a team let's the opponents score, affects their odds of winning.
- For this simple example, we will focus on data from one team: SAS (San Antonio Spurs).
- The data is in the file `nba_games_stats_reduced.csv` on Sakai.
- Ideally, we should use more information (and that data is actually available) to predict wins but let's continue for illustrative purposes.
- You will get to practice with the full data soon.

PREDICTING NBA WINS

```
nba <- read.csv("data/nba_games_stats_reduced.csv",header=T)
nba <- nba[nba$Team=="SAS",]
colnames(nba)[3] <- "Opp"
nba$win <- rep(0,nrow(nba)); nba$win[nba$WINorLOSS=="W"] <- 1
nba$win <- as.factor(nba$win)
head(nba); dim(nba)
```

```
##      Team WINorLOSS Opp win
## 165  SAS          W 100  1
## 166  SAS          L  94  0
## 167  SAS          W  92  1
## 168  SAS          L  98  0
## 169  SAS          L 100  0
## 170  SAS          W  85  1
```

```
## [1] 328  4
```

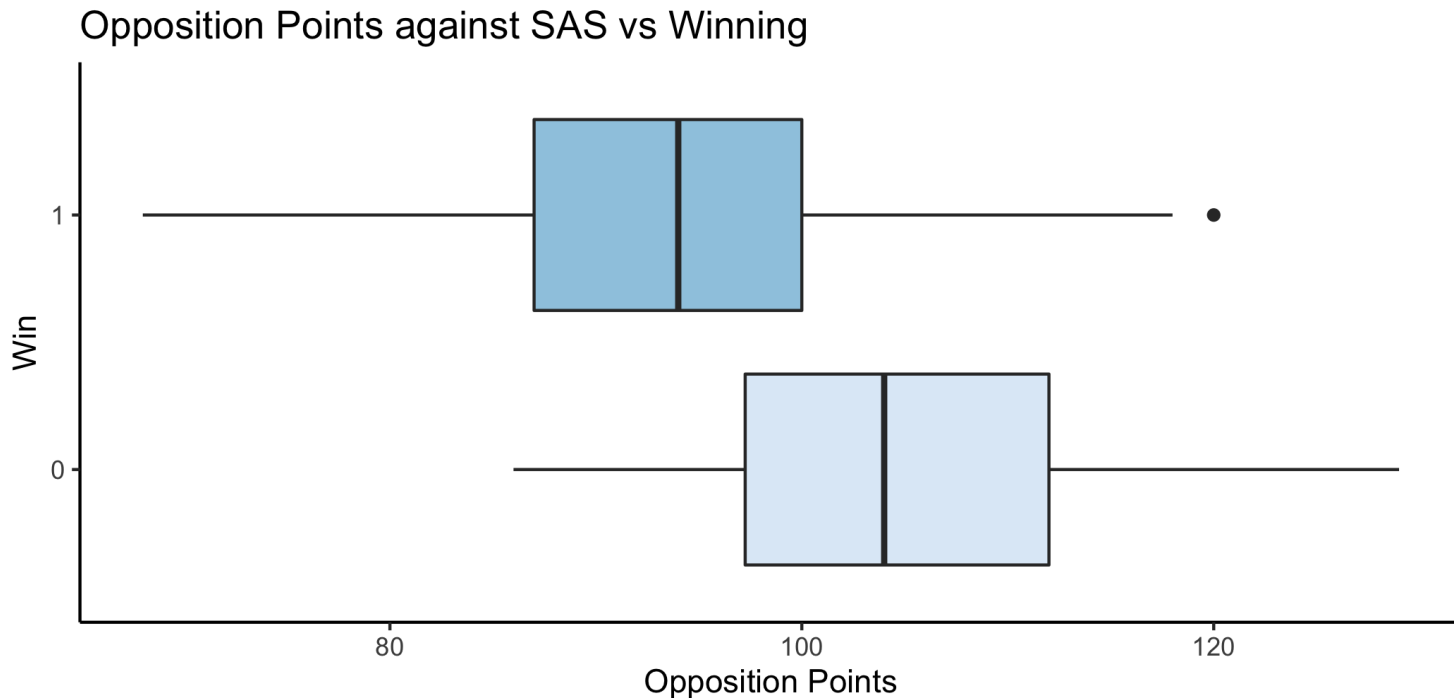
```
summary(nba)
```

```
##      Team          WINorLOSS          Opp          win
## Length:328      Length:328      Min.   : 68.00    0: 98
## Class :character Class :character 1st Qu.: 90.00    1:230
## Mode  :character Mode  :character Median  : 97.00
##                               Mean   : 96.97
##                               3rd Qu.:104.00
##                               Max.   :129.00
```

PREDICTING NBA WINS

Only one predictor so not much to do in terms of EDA. We can look at

```
ggplot(nba,aes(x=win, y=Opp, fill=win)) +  
  geom_boxplot() + coord_flip() +  
  scale_fill_brewer(palette="Blues") +  
  labs(title="Opposition Points against SAS vs Winning",y="Opposition Points",x="Win") +  
  theme_classic() + theme(legend.position="none")
```



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$$\text{win}_i | \text{Opp}_i \sim \text{Bernoulli}(\pi_i); \quad \log\left(\frac{\pi_i}{1 - \pi_i}\right) = \beta_0 + \beta_1 \text{Opp}_i$$

```
nbareg <- glm(win~Opp,family=binomial(link=logit),data=nba); summary(nbareg)
```

```
##
## Call:
## glm(formula = win ~ Opp, family = binomial(link = logit), data = nba)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.2760  -0.7073   0.4454   0.7902   1.9593
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 13.31989    1.66935   7.979 1.47e-15
## Opp         -0.12567    0.01655  -7.594 3.11e-14
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 400.05  on 327  degrees of freedom
## Residual deviance: 313.42  on 326  degrees of freedom
## AIC: 317.42
##
## Number of Fisher Scoring iterations: 5
```

PREDICTING NBA WINS

Same output re-presented:

```
stargazer(nbareg,type = "html", header = FALSE,single.row = TRUE)
```

	<i>Dependent variable:</i>
	win
Opp	-0.126 ^{***} (0.017)
Constant	13.320 ^{***} (1.669)
Observations	328
Log Likelihood	-156.709
Akaike Inf. Crit.	317.417
<i>Note:</i>	* p<0.1; ** p<0.05; *** p<0.01

For every additional point an opponent scores against SAS in a game, the odds of winning decreases by approximately 12%, since $\exp(-0.126) = 0.88$.

PREDICTING NBA WINS

```
#Let's mean-center the opposition points for interpretation.  
nba$Opp_cent <- nba$Opp - mean(nba$Opp)  
nbareg <- glm(win~Opp_cent,family=binomial(link=logit),data=nba)  
stargazer(nbareg,type = "html", header = FALSE,single.row = TRUE)
```

	<i>Dependent variable:</i>
	win
Opp_cent	-0.126 ^{***} (0.017)
Constant	1.134 ^{***} (0.151)
Observations	328
Log Likelihood	-156.709
Akaike Inf. Crit.	317.417
<i>Note:</i>	* p<0.1; ** p<0.05; *** p<0.01

The odds of SAS winning an nba game during this period, when the opposition scores approximately 97 points, is approximately 3.11, that is, $\exp(1.134)$.

PREDICTING NBA WINS

Confidence intervals for the coefficients. Remember that this is on the log-odds scale.

```
confint.default(nbareg) #Asymptotic
```

```
##                2.5 %        97.5 %  
## (Intercept)  0.8370288  1.43070311  
## Opp_cent    -0.1581094 -0.09323567
```

```
confint(nbareg) #Based on the profile-likelihood
```

```
## Waiting for profiling to be done...
```

```
##                2.5 %        97.5 %  
## (Intercept)  0.8462671  1.44156134  
## Opp_cent    -0.1599671 -0.09488784
```

Can you interpret the intervals?

PREDICTING NBA WINS

Let's transform to the odds scale.

```
exp(confint.default(nbareg)) #Asymptotic
```

```
##                2.5 %    97.5 %  
## (Intercept) 2.3094947 4.1816383  
## Opp_cent    0.8537564 0.9109788
```

```
exp(confint(nbareg)) #Based on the profile-likelihood
```

```
## Waiting for profiling to be done...
```

```
##                2.5 %    97.5 %  
## (Intercept) 2.3309296 4.2272909  
## Opp_cent    0.8521718 0.9094749
```

Can you interpret the intervals?

PREDICTING NBA WINS

We can get the predicted probabilities for the observed cases.

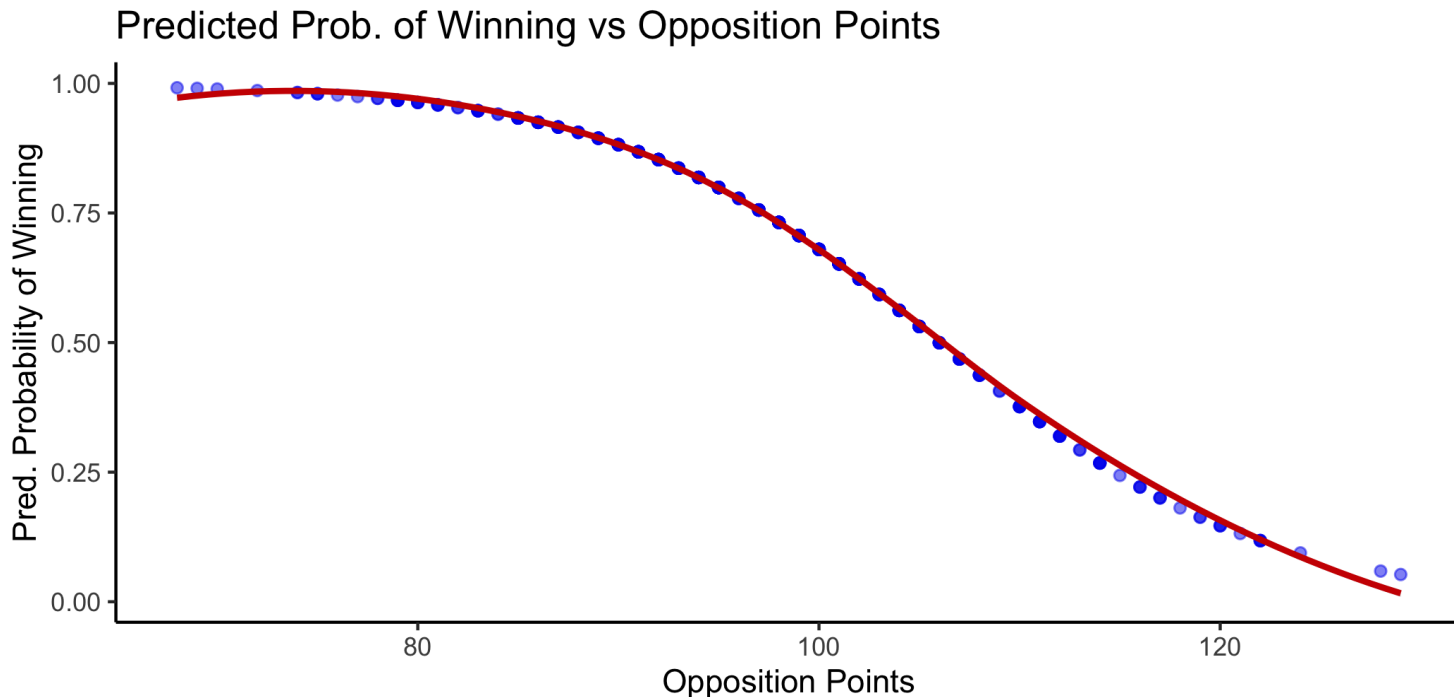
```
nba$predprobs <- predict(nbareg,type="response")  
#use predict(logreg, type="link") for the logit scale  
nba[1:20,]
```

##	Team	WINorLOSS	Opp	win	Opp_cent	predprobs
## 165	SAS	W	100	1	3.033537	0.6797523
## 166	SAS	L	94	0	-2.966463	0.8185670
## 167	SAS	W	92	1	-4.966463	0.8529607
## 168	SAS	L	98	0	1.033537	0.7318401
## 169	SAS	L	100	0	3.033537	0.6797523
## 170	SAS	W	85	1	-11.966463	0.9332502
## 171	SAS	W	100	1	3.033537	0.6797523
## 172	SAS	W	80	1	-16.966463	0.9632468
## 173	SAS	L	94	0	-2.966463	0.8185670
## 174	SAS	W	75	1	-21.966463	0.9800514
## 175	SAS	W	90	1	-6.966463	0.8817762
## 176	SAS	W	92	1	-4.966463	0.8529607
## 177	SAS	W	87	1	-9.966463	0.9157825
## 178	SAS	W	100	1	3.033537	0.6797523
## 179	SAS	W	104	1	7.033537	0.5621626
## 180	SAS	W	89	1	-7.966463	0.8942617
## 181	SAS	W	103	1	6.033537	0.5928153
## 182	SAS	L	95	0	-1.966463	0.7991510
## 183	SAS	W	101	1	4.033537	0.6518001
## 184	SAS	W	101	1	4.033537	0.6518001

PREDICTING NBA WINS

Useful to examine a plot of predicted probabilities by x , that is, opposition points.

```
ggplot(nba,aes(x=Opp, y=predprobs)) +  
  geom_point(alpha = .5,colour="blue2") +  
  geom_smooth(col="red3") + theme_classic() +  
  labs(title="Predicted Prob. of Winning vs Opposition Points",x="Opposition Points",y="Pr
```



WHAT'S NEXT?

MOVE ON TO THE READINGS FOR THE NEXT MODULE!