

IDS 702: MODULE 1.10

BRINGING THE MLR PIECES TOGETHER I (ILLUSTRATION)

DR. OLANREWAJU MICHAEL AKANDE

DIAMONDS DATA

- A diamond's value is often determined using four factors known as the 4Cs: color, clarity, cut (certification) and carat weight.
 - Color: evaluation based on absence of color; how pure the diamond is. **This is a categorical variable with 6 levels.**
 - Clarity: evaluation based on absence of blemishes. **This is a categorical variable with 5 levels.**
 - Certification: how well the diamond is cut; how well a diamond's facets interacts with light. **This is a categorical variable with 3 levels.**
 - Carats: carat weight measuring how much the diamond weighs. **This is a continuous variable.**
- We will use some data to draw inference about how these factors affect a diamond's price (**continuous**).
- You can read more about the 4Cs [here](#).

MULTIPLE REGRESSION OF DIAMONDS DATA

- A good starting model is

$$y_i = \mathbf{x}_i \boldsymbol{\beta} + \epsilon_i; \quad \epsilon_i \sim N(0, \sigma^2).$$

where y_i is the price for observation i , and \mathbf{x}_i is the vector containing the corresponding values for Carats, Color, Clarity, and Certification.

- Alternatively, write

$$\begin{aligned} \text{Price}_i = & \beta_0 + \beta_1 \text{Carats}_i + \sum_{j=2}^6 \beta_{2j} 1[\text{Color}_i = j] + \sum_{j=2}^5 \beta_{3j} 1[\text{Clarity}_i = j] \\ & + \sum_{j=2}^3 \beta_{4j} 1[\text{Certification}_i = j] + \epsilon_i; \quad \epsilon_i \sim N(0, \sigma^2). \end{aligned}$$

- Can also write

$$\begin{aligned} \widehat{\text{Price}}_i = & \hat{\beta}_0 + \hat{\beta}_1 \text{Carats}_i + \sum_{j=2}^6 \hat{\beta}_{2j} 1[\text{Color}_i = j] + \sum_{j=2}^5 \hat{\beta}_{3j} 1[\text{Clarity}_i = j] \\ & + \sum_{j=2}^3 \hat{\beta}_{4j} 1[\text{Certification}_i = j]. \end{aligned}$$

MULTIPLE REGRESSION OF DIAMONDS DATA

- This is just a candidate model.
- We will go through the full (almost!) modeling process and we will see if this model makes sense or if we need to make changes to it.
- We will start by doing EDA, all the way down to model assessment, including investigating multicollinearity.
- We will explore transformations, polynomial forms, interactions, etc.
- The data is in the file `diamonds.csv` on Sakai.

MOVE TO THE R SCRIPT HERE.

WHAT'S NEXT?

MOVE ON TO THE READINGS FOR THE NEXT MODULE!